

1 **Calibrating multi-frequency acoustic backscatter systems for studying near-bed**
2 **suspended sediment transport processes**

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Abstract

The utilisation of sound backscattered from sediments in suspension, to measure profiles of near-bed particle size and concentration, has been gaining increasing acceptance and usage by sedimentologists and coastal engineers over the past two decades. To obtain the sediment parameters from the backscattered signal requires an inversion to be conducted on the signal and this necessitates a system calibration. The calibration can be carried out by detailed acoustic and electronic measurements, or alternatively by measuring the backscattering from suspensions with known scattering characteristics. Here we explore the latter approach and describe in some detail the calibration of a triple frequency acoustic backscatter system. The aim is to provide coastal scientists involved in using acoustics as a tool for sediment transport research, with a clear exposition of the calibration process. Suspensions of glass spheres of varying particle size were used as the calibration scatterers. To interpret the signal backscatter from the suspension of glass spheres a simple model for sphere scattering is presented. The results show that consistent calibration results can be obtained in a relatively simple and robust manner.

I Introduction

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52

53 The processes of near-bed sediment transport can be thought of as dynamic feedback
54 interactions between the bed, the flow and the mobile sediments. In recent years acoustic
55 instrumentation has been increasingly used to measure, co-located and simultaneously,
56 these three components of this inter-related sediments triad. Acoustics has gained this
57 role because of its capability to profile non-intrusively, with high temporal and spatial
58 resolution, the three components. A review by Thorne and Hanes, 2002, detail some of
59 these applications. In the present study we focus on the use of multi-frequency acoustic
60 backscattering for measuring near-bed profiles of suspended particle size and
61 concentration and in particular the calibration of such systems. To extract the suspended
62 sediment parameters from the backscattered signal necessitates an inversion to be
63 conducted on the acoustic signal. To carry out the inversion requires a calibration of the
64 acoustic backscatter system. While there is a wide variety of publications (Hay and Sheng
65 1992, Hampton et al 1998, Vincent and Hanes 2000, Rose and Thorne 2001, Green et al
66 2004, Dohmen-Janssen and Hanes 2005 and recent commercially available systems
67 Smerdon 2006) on the use of acoustic backscatter systems, ABS, to measure profiles of
68 sediment concentration and size, there is little published literature on how to perform the
69 calibrations of these systems. It was therefore considered appropriate and timely to
70 examine the calibration of such systems. The aim here is to provide coastal engineers and
71 scientist, who are increasingly using such instruments as a tool for sediment studies, with
72 a clear description of the calibration process, so that data collected with an ABS can be
73 accurately and correctly interpreted.

74

75 The calibration of a multi-frequency ABS can be carried out by measuring the electronic
76 response of the system, in conjunction with measurements of the transmit and receive
77 sensitivities and beam patterns of the acoustic transducers, Thorne and Hardcastle, 1997.
78 These are time consuming operations and the acoustic component of the calibration
79 requires specialist equipment that would not normally be readily available in most
80 sedimentary laboratories. The alternative to such a calibration is to measure the
81 backscattering from a suspension with known scattering characteristics. Such a
82 measurement automatically incorporates both the electronic and acoustic components of

83 the calibration. The choice of scatterers in suspension for the calibration is crucial. It
84 might be considered that natural sandy sediments would be an appropriate choice, given
85 that ABS's have generally been deployed above sandy beds in the marine environment,
86 however, this is not the case. If, for example, natural sediments were used, the measured
87 system calibration constant would only be valid for that particular sediment site and size
88 distribution. This is because of the detailed variable scattering characteristics due to the
89 precise shape and mineralogy of natural sediments. (Schaafsma and Hay 1997; Thorne
90 and Buckingham 2004). This is not to say there is no theoretical framework for the
91 interaction of sound with suspended sediments, there is, see Thorne and Hanes 2002. It is
92 the sandy sediment scattering characteristics given in such papers which are used in the
93 multi-frequency ABS inversion to obtain profiles of particle size and concentration.
94 However, the description of the interaction of sound with sandy suspensions is not as
95 precise as that of spheres, and never will be, because of the uncertainty introduced by the
96 particles being non-spherical and irregular in shape. Therefore in the present study the
97 calibrations were conducted using suspensions of spheres. The scattering properties of
98 spheres are well documented and an exact solution exists (Gaunaud and Uberall, 1983).
99 Spheres provide the correct value for the system constant, because their scattering
100 properties are precisely known and therefore the system constant can be decoupled from
101 the scattering properties of the suspension. As will be seen below, the exact sphere
102 solution is moderately complicated, however, here we present a new simple
103 approximation to the exact solution, which can be easily evaluated and used for ABS
104 calibration purposes.

105

106 Many sedimentary laboratories have facilities for generating suspensions for instrument
107 calibration and for studying suspended sediment processes. Therefore the approach
108 adopted here should have broad appeal. For the present study a homogeneous suspension
109 of sediments were generated in a sediment tower constructed for calibration and sediment
110 scattering studies. The tower provided a homogeneous suspension over about one metre.
111 Calibration of a triple frequency ABS was carried out by measuring the backscattered
112 signal from a suspension of sediments. The sediments used were glass spheres; these are
113 inexpensive and readily obtained. Their scattering properties have been measured and

114 good agreement obtained with theoretical predictions; Hay 1991, Thorne et al 1992,
115 Schaafsma and Hay 1997. Here results are reported on calibrations conducted in a
116 sediment tower on suspensions of glass spheres with particle sizes ranging in radius from
117 50-400 μm . The procedure for the calibration is explained in some detail so that the
118 approach can be readily understood. The outcomes from the measurements are discussed
119 and an assessment of the accuracy of the calibration is considered.
120

II Theory

Here we provide the background theory to incoherent scattering from a suspension of sediments and how this is used to obtain the system constant, from a series of simple backscattering measurements. The description of the backscattering from suspended sediments is now well developed (Sheng and Hay 1988, Hay 1991, Hay and Sheng 1992, Thorne and Campbell 1992, Thorne et al 1993, Thorne and Hardcastle 1997) and the root-mean-square backscattered signal, V_{rms} , from a homogeneous suspension can be written as

$$V_{\text{rms}} = \frac{K_s K_t M^{1/2}}{r\psi} e^{-2r\alpha} \quad (1)$$

$$K_s = \frac{f}{\sqrt{\rho_s a_s}}, \quad \alpha = \alpha_w + \frac{3\chi M}{4a_s \rho_s}$$

The term K_s contains the sediment backscattering properties; ρ_s is the sediment grain density, a_s is the particle radius of the sediment in suspension and f is known as the form function and describes the backscattering characteristics of the particles in suspension. The term α_w is the attenuation due to water absorption, M is the concentration of sediment in suspension, r is the range from the transducer, ψ accounts for the departure from spherical spreading within the transducer near-field (Downing et al 1995) and χ is known as the normalized total scattering cross-section and describes the scattering attenuation characteristics of the suspension. For fixed settings K_t is a system constant and its measurement is the focus of this paper. It is necessary to establish the value of K_t , as a prerequisite, for the interpretation of backscatter data collected in the marine environment. If the system is operating in its linear region, that is the recorded signal is linearly proportional to the backscattered pressure, and if account has been taken of any time varied gain applied to the system, then a calibration can be obtained by a single measurement using a suspension of known particle size and concentration. By simply rearranging equation (1) and considering measurements made in the far-field of the ABS

151 transducers, that is where $r > A/\lambda$, giving $\psi=1$, and where A is the area of the transducer
 152 radiating aperture, we obtain

$$153 \quad K_t = \frac{V_{rms} r}{K_s M^{1/2}} e^{2\alpha r} \quad (2)$$

154
 155 V_{rms} is the measured backscattered signal at range r , a_s can be measured by sieving the
 156 sediments in suspension, ρ_s can be readily measured and f , for spheres, is given below in
 157 equation (3a), hence K_s is known. The attenuation in the exponent, α , is made up of two
 158 components; α_w which can be taken from tables (eg Kaye, and Laby, 1986.) and χ which
 159 is given by equation (3b). M can be obtained by direct sampling of the suspension. Hence
 160 all the parameters are known on the right hand side of equation (2) for the evaluation of
 161 K_t .

162
 163 The exact solutions for f and χ , for sphere scattering, are given by

$$164 \quad f = \left| \frac{2}{ix} \sum_{n=0}^{n=\infty} (-1)^n (2n+1) b_n \right| \quad (3a)$$

$$166 \quad \chi = \left| \frac{-2}{x^2} \sum_{n=0}^{n=\infty} (2n+1) \text{Re}(b_n) \right| \quad (3b)$$

168
 169 Where b_n is a moderately complex function composed of spherical Bessel and Hankel
 170 functions of the first kind and their derivatives (Gaunard and Uberall, 1983), Re denotes
 171 taking the real part of the complex expression and $x=ka_s$ where $k=2\pi/\lambda$ and λ is the
 172 wavelength of the sound in water. Shown in Figure 1, and represented by the dashed
 173 lines, are calculations for f and χ , obtained using equation (3), for a suspension of glass
 174 spheres of uniform particle size. The values used in the calculation for the glass spheres
 175 were; compressional and shear wave velocities respectively of 5550 ms^{-1} and 3545 ms^{-1} ,
 176 with a density of 2500 kgm^{-3} . For water the values used for density and sound velocity
 177 were 1000 kgm^{-3} and 1480 ms^{-1} . As can be seen in figure 1, f is quite variable in form
 178 above $x=5$, with a series of sharp dips associated with spherical resonances of the spheres
 179 in suspension. Alternatively χ is relatively simple in structure. The solid lines in figure 1
 180 were calculated for a suspension with a $1/4\phi$ ($\phi = -\log_2 d$ where d is the particle diameter in

181 millimetres) size fraction. The size range covered by $\frac{1}{4}\phi$ sieves is nominally $a_s \pm 0.09a_s$.
 182 Introducing even this relatively narrow size range into the suspension significantly
 183 reduces the dips in f , with the result that its structure is somewhat simplified. The impact
 184 of the size range on χ is essentially minimal. The simplification in the form of f allows
 185 the suspension scattering characteristics to be represented by the following easily
 186 evaluated expressions.

$$187 \quad f = \frac{\zeta x^2}{1.17 + 0.95x^2} \quad (4a)$$

$$188 \quad \zeta = (1 - 0.5e^{-((x-1.5)/0.5)^2})(1 + 0.4e^{-((x-1.5)/3.0)^2})(1 - 0.5e^{-((x-5.9)/0.7)^2})$$

189

$$190 \quad \chi = \frac{0.24\phi x^4}{0.7 + 0.3x + 2.1x^2 - 0.7x^3 + 0.3x^4} \quad (4b)$$

191

$$192 \quad \phi = 1 - 0.4e^{-((x-5.5)/2.5)^2}$$

193

194 Figure 2 shows comparisons of equation (4), which is a simplified empirical expression
 195 representing the solid lines in figure 1, with the measurements (Thorne and Buckingham
 196 2004, Schaafsma and Hay 1997) conducted on suspensions of glass spheres sieved into
 197 $\frac{1}{4}\phi$ size fractions. It can readily be seen that for the range of x considered, $x=0-8$, the
 198 above simple equations accurately describes the scattering characteristics for $\frac{1}{4}\phi$ sieved
 199 suspensions of glass spheres. If suspensions other than $\frac{1}{4}\phi$ sieved were used, equation (4)
 200 would have to be modified. In the rest of the paper it is equation (4) which is used to
 201 calculate f and χ for the evaluation of the equation (2) to obtain K_t .

202

III Instrumentation

203

204

205 (i) Tower

206 Figure 3 shows the sediment tower used for the calibration measurements. It primarily
207 consisted of a 2.15 m transparent Perspex vertical tube, with a diameter of 0.3 m and with
208 mixing and re-circulating units. The main objective of the tower's design was to generate
209 a homogenous suspension of sediments over about a metre in length, which remained
210 constant over time, and did not contain micro-bubbles, since the latter are significant
211 acoustic scatterers in their own right. Once the tower was filled with a suspension, bilge
212 pumps were used to extract water and sediment from the bottom of the tower and
213 deliver it back to the top of the tower through a 0.05 m diameter pipe. Two bilge pumps,
214 pumping side by side, operating at approximately 50% of their maximum capacity were
215 chosen for this function. Operating in this mode prevented pump cavitation and thereby
216 reduced the possibility of introducing air into the system through the pumping
217 mechanism. Also the two pumps generated sufficient flow in the return pipe to ensure the
218 sediments extracted with the water from the bottom of the tower were returned to the top.
219 At the top of the tower the suspension was re-introduced below the upper water surface,
220 open to the atmosphere, through a mixing chamber, designed to homogenise the
221 suspended sediments within the tower, without the entrainment of air. The upper mixing
222 arrangement provided a degree of homogeneity, however, further mixing was required to
223 obtain uniformity over a metre. Through a method of trial and error a rotating mixing unit
224 composed of a turbulence grid, impeller and propeller which generated an upward mixing
225 turbulent flow was arrived at. This combination of mixing elements provided a bubble
226 free uniform suspension over the central portion of the tower.

227

228 Intermittently the tower required cleaning and was refilled with water from the mains
229 supply. In such cases, due to the presence of micro-bubbles in the fresh water, a period of
230 hours to days was allowed to elapse, with the system running, but with no sediment
231 present, to vent off the air in the water to the atmosphere through the open top of the
232 tower. When the backscatter background signals reduced to levels comparable with the
233 electronic noise floor of the ABS, degassed wetted sediments were introduced into the

234 system. Typically suspended sediment backscatter recordings of about one hour were
235 used to obviate the impact of any short term fluctuations in the suspended concentration
236 and to obtain accurate values for V_{rms} . The backscattered signal has an amplitude that is
237 Rayleigh distributed (see Thorne et al 1993) with a standard error in V given
238 approximately by $V_{\text{rms}}/(2\sqrt{n})$, where n is the number of independent backscatter
239 measurements. Therefore if the aim is to achieve 1% accuracy in V_{rms} , 2500 independent
240 profiles have to be collected and the root-mean-square average formed.

241

242

243 (ii) Acoustic backscatter system

244 The system calibrated was a triple frequency ABS with the transducers operating in
245 transceiver mode at 1.0 MHz, 2.0 MHz and 4.0 MHz, having nominal -3dB half
246 beamwidths respectively of 2° , 2° , and 1° and a transmitted pulse length of 0.02 m. The
247 transducers were mounted near the top of the tower and their beams were directed
248 vertically downwards. The system measured the amplitude envelope of the backscattered
249 signal at 0.01 m intervals over a range of 1.28 m. Although in the marine environment the
250 ABS system interleaved the three frequencies with a pulse repetition frequency of 128
251 Hz, to obtain high temporal resolution measurement of the suspended sediments, for the
252 acoustically reverberant environment of the tower the pulse repetition frequency was
253 reduced to 4 Hz, to allow sufficient absorption of the sound pulse, by the water, to
254 prevent interference between consecutive transmissions.

255

256 (iii) Sediments

257 The suspension used for the calibration was composed of glass spheres sieved into $\frac{1}{4}\phi$
258 size fractions and covering a particle size range of $a_s=50-400 \mu\text{m}$. The glass was soda
259 glass and had the physical characteristics given in the ‘Theory’ section above. Figure 4
260 shows a typical scanning electron micrograph of the sediment. The glass spheres can be
261 seen to be nominally spherical in shape, although it can readily be seen that there was
262 some departure from sphericity and with odd nodules and paired particles being present
263 in the batch. However, even though the glass spheres were not perfectly spherical, the

264 data presented in figure 2 shows the scattering behavior of suspensions of glass particles
265 is well represented by a sphere scattering model.

266

267 (iv) Suspension homogeneity

268 As shown in figure 3, to generate a homogeneous suspension a combination of
269 recirculation using pumps and stirring was employed. To assess the homogeneity of the
270 suspension in the tower experiments were conducted using suspensions of glass spheres
271 with $a_s=115, 137$ and $195 \mu\text{m}$. Siphoned samples of the sediments were collected
272 between 0.3-0.8 m below the transducers, and located on the central vertical axis of the
273 tower, at 0.07 m from the axis, and at 0.14 m from the axis, the latter was within 0.01m of
274 the tower wall. Known volumes of water were extracted, passed through a $10 \mu\text{m}$ aperture
275 net filter, and the retained sediments dried and weighed. The concentration was then
276 calculated as the dried mass divided by the volume of water extracted. The resultant
277 measured concentrations are given in figure 5. The data clearly show the suspended
278 sediments were homogeneous both across the tower and vertically. There was no
279 significant difference with sediment size and the individual pump samples were generally
280 within about $\pm 10\%$ of the mean concentration of the suspension.

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IV Measurements and results

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288

289 Backscatter measurements were collected on suspensions of glass spheres sieved into $\frac{1}{4}\phi$
290 size fraction over a range of particle radii between $a_s=50-400 \mu\text{m}$. The concentration in
291 the tower was kept relatively constant for each size fraction and was normally in the
292 range $0.4-0.6 \text{ kgm}^{-3}$. The normal experimental procedure was to take background
293 readings for several minutes in clear water, add wetted and degassed sediment to the
294 tower, allow the mixture to homogenise over a period of about one hour, record data for
295 of the order of one hour, take pumped samples to assess the concentration and
296 homogeneity and then remove the sediment from the tower using a conical fine nylon
297 mesh, of aperture size $20 \mu\text{m}$, placed in the top of the tower. The tower was then ready
298 for another experiment and the whole procedure was repeated.

299

300 A typical example of the relative root-mean-square backscatter signal, V_{rms} , is shown in
301 figure 6. This data was collected using $M=0.58 \text{ kgm}^{-3}$ and $a_s=115 \mu\text{m}$. The first 0.1 m
302 data is not shown because this was contaminated by crosstalk between the transmitter and
303 receiver during transmission. The results show a decreasing backscattered signal with
304 range due to the r^{-1} term in equation (1) and with increasing signal reduction with
305 frequency due to increasing water absorption and sediment attenuation. To obtain
306 backscatter profiles as smooth as shown in figure 6, 5000 independent profiles were
307 collected and the root-mean-square average formed.

308

309 Using the type of data shown in figure 6, equation (2) was evaluated for a number of
310 different $\frac{1}{4}\phi$ size fractions using the sphere scattering model given by equation (4).
311 Ideally the value calculated for K_t should be independent of range, particle size and
312 concentration, since it is a system constant and not dependent upon the suspension.
313 Figure 7 shows profiles of K_t with range between $0.1-1.1 \text{ m}$ ($0.2-1.1 \text{ m}$ for the 1.0 MHz
314 due to crosstalk) for three different particle sizes. The error bars were derived from
315 repeating experiments on the same particle size. Although there are differences in the
316 results between the different particle sizes, they are comparable with those obtained by
317 carrying out repeat experiments on the same size particle; therefore there was no

318 systematic variation with particle size. As can be seen, essentially the same is true with
319 range; the value for K_t does not have any significant trend with range. The latter also
320 supports the conclusion drawn from figure 5 that the suspension was homogeneous; since
321 if this were not the case, K_t would not be constant with range. Although not shown here
322 for brevity, measurements made of K_t with another multi-frequency ABS showed no
323 trends with concentration. To assess all the data sets, the values for K_t were averaged
324 over the range 0.2-0.8 m and the results for all the particle sizes are plotted in figure 8.
325 The solid line in the figures is the K_t value averaged over the all the size fractions and the
326 dashed lines are 10% values about this line. As can be seen, in keeping with figure 7,
327 there is no systematic variation of K_t with a_s , which is exactly what should be the case if
328 equation (4) accurately represents the acoustic scattering properties of a suspension of
329 glass spheres sized into $\frac{1}{4}\phi$ fractions. In general the data do lay between the 10% dashed
330 lines. There does seem to be somewhat more variability in the measurements above
331 $a_s=250\mu\text{m}$ and this is ascribed to the difficulty in maintaining the sediment in suspension
332 for the larger size fractions, however, even in this regime the results remain consistent.
333 For the smaller size fractions, below $a_s= 200 \mu\text{m}$, with the odd exception, for example
334 $164 \mu\text{m}$ at 2 MHz, the results are very consistent. It is not readily apparent why the odd
335 outliers occur, since the discrepancies are not consistent across the three frequencies. The
336 values for K_t were recomputed using the exact solutions of equation (3) with account
337 taken of the size range within a $\frac{1}{4}\phi$; however, there were no significant differences in the
338 resulting K_t values. Therefore the simplified sphere model was not introducing any
339 significant errors. At present, these relatively small discrepancies, in what is generally a
340 consistent calibration series, cannot be explained other than due to experimental error.
341

V Discussion and conclusion

342

343

344 The application of acoustic backscattering to the measurement of suspended sediment
345 concentration and particle size has become a relatively common technique. The
346 development of ABS systems from their initial development by and for academic
347 institutions, to the production of commercially developed systems is allowing for the
348 broader application of this acoustic technology. To fully take advantage of multi-
349 frequency ABS and obtain accurate quantitative measurements of particle size and
350 concentration requires calibration of the system. As noted in the introduction the
351 calibration can be carried out by measuring the electronic and acoustic response of the
352 system. This requires specialised equipment for the acoustic component of the calibration
353 and such equipment would not normally be available in a sedimentary laboratory.
354 However, such laboratories often have systems to generate suspensions of sediments,
355 both for instrument calibration purposes and for the study of sediment transport
356 processes. Therefore the approach adopted in the present paper has been to utilise the
357 scattering from suspensions of sediments to calibrate an ABS.

358

359 As discussed in the 'Introduction', it could be thought that natural sediments should be
360 used for the calibration, however, this essentially leads to a calibration only applicable to
361 the sediments used for the calibration. Therefore the material used for the suspensions
362 was glass spheres. These are readily obtained in the size range required and are
363 inexpensive. The scattering properties of glass spheres have been well documented and
364 are in accord with the general theory of sphere scattering given in equation (3). For all
365 practical circumstances when suspensions are being generated in the laboratory for
366 calibration, the glass spheres will be divided into separate size fractions by sieving.
367 Therefore the approach adopted here was to take advantage of the impact a spread of
368 particle sizes in suspension had on the complicated resonances associated with equation
369 (3), and provide very simple expressions for the backscattering and attenuation of
370 suspensions of glass spheres sieved into $\frac{1}{4}\phi$ size fractions. Equation (4) essentially
371 provides the non-specialist in acoustics with readily usable scattering expressions for
372 calibrating an ABS system. The veracity of the equation (4) was assessed with published

373 laboratory measurements and good agreement was obtained. To carry out the calibration
374 a sediment tower was constructed, this used a mixture of pumping and mixing to generate
375 a homogeneous suspension. The construction of the tower was not particularly
376 complicated and its use is straightforward. Using a range of sediments in the tower, with
377 $\frac{1}{4}\phi$ size fractions between 50-400 μm , a series of measurements of K_t were collected. The
378 results showed that profiles of K_t were nominally constant with range and particle size
379 and the deviations from the ideal single value were generally close to the limits of the
380 accuracy of the measurement technique. The K_t values for the individual size fractions
381 were generally within $\pm 10\%$ of the global mean obtained by averaging over all the size
382 fractions. The final average value for the normalized standard error, $\sigma_e(K_t)/K_t$, for each
383 frequency, was close to 2%. Improvements to achieve further accuracy are not warranted
384 for the acoustic inversion because the scattering properties of marine sediments are not
385 known to this level. Indeed using three fractions reasonably well separated in size should
386 be adequate; this provides a standard error for K_t of about 5% and the three sizes offers
387 some protection against an erroneous K_t value which could possibly arise if only one size
388 fraction was used.

389

390 On a final note, although the calibration of acoustic Doppler velocity meters, ADV's and
391 higher frequency short range acoustic Doppler current profilers, ADCP's, is not the focus
392 of the present paper, the methodology of using homogeneous suspensions of spherical
393 scatters can be used to obtain a similar calibration constant for such systems (Deines
394 1999). However, since the calibration present here is for a linear system, appropriate
395 accounting for any logarithmic amplification and/or time varying gain used in such
396 systems is required to derive the correct K_t value.

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447

448 **Figure captions**

449

450 Figure 1. Predictions for f and χ with x , calculated using equation (3), for a suspension of
451 uniform particle size (---) and with a $\frac{1}{4}\phi$ size fraction (—).

452

453 Figure 2. Comparison of f and χ with x , calculated using equation (4), with measured
454 values (●) obtained using $\frac{1}{4}\phi$ size fractions.

455

456 Figure 3. Diagram of the sediment tower used for the calibrations.

457

458 Figure 4. Scanning electron micrograph of the glass sphere sediments used in the
459 calibration study.

460

461 Figure 5. Measurements of the variation of concentration across the tower and with
462 range; for $a_s = 0-115 \mu\text{m}$, $x-137 \mu\text{m}$ and $+195 \mu\text{m}$.

463

464 Figure 6. Measurements of the relative backscatter signal with range in the tower; (●) 1.0
465 MHz, (o) 2.0 MHz and (x) 4.0 MHz for $a_s = 115 \mu\text{m}$ and $M = 0.58 \text{ kgm}^{-3}$.

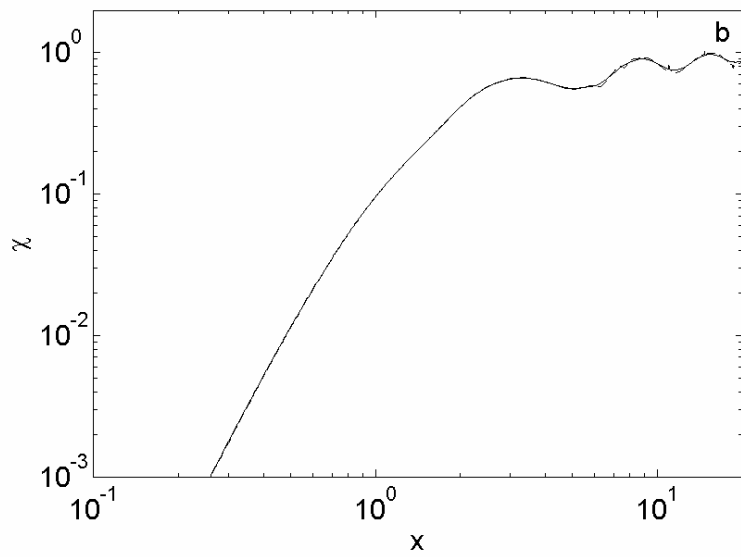
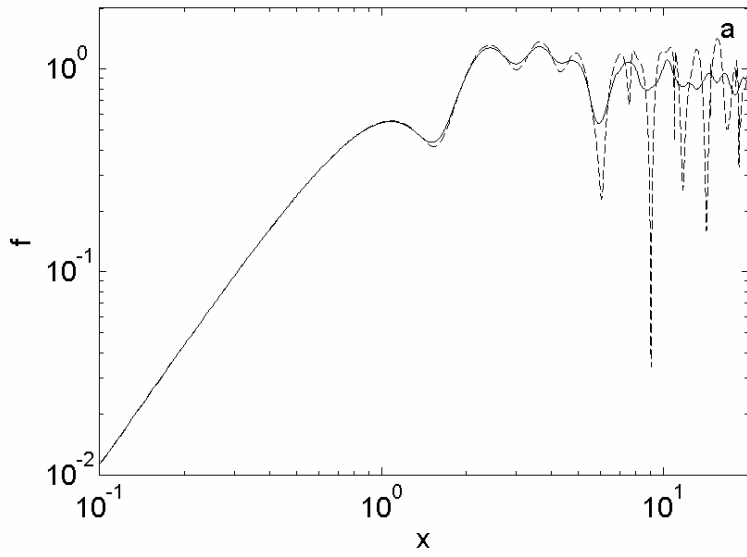
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467 Figure 7. Measurements of K_t with range for $a_s = 68$ (●), 115 (o) and 195 (+) μm , at a) 1.0
468 MHz, K_{t1} , b) 2.0 MHz, K_{t2} and c) 4.0 MHz, K_{t4} .

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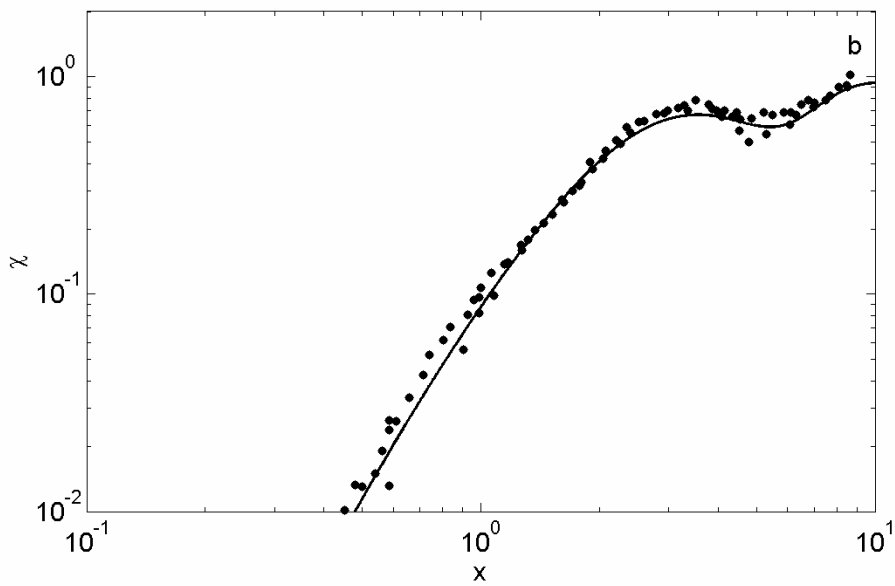
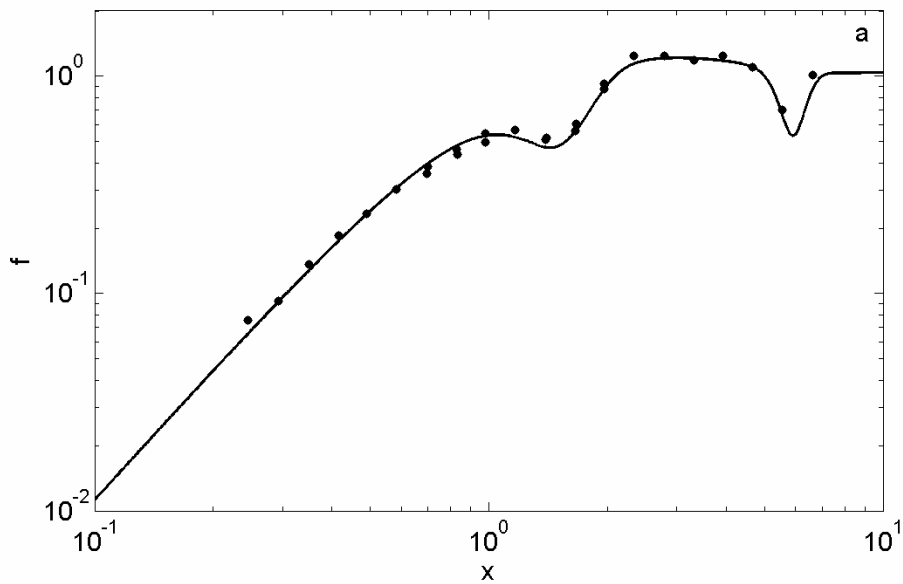
470 Figure 8. Mean values for K_t between 0.2-0.8 m for $\frac{1}{4}\phi$ size fractions between 50-400
471 μm . The solid line is the K_t value averaged over the all the size fractions and the dashed
472 lines are $\pm 10\%$ values about this line. a) 1.0 MHz, K_{t1} , b) 2.0 MHz, K_{t2} and c) 4.0 MHz,
473 K_{t4} .

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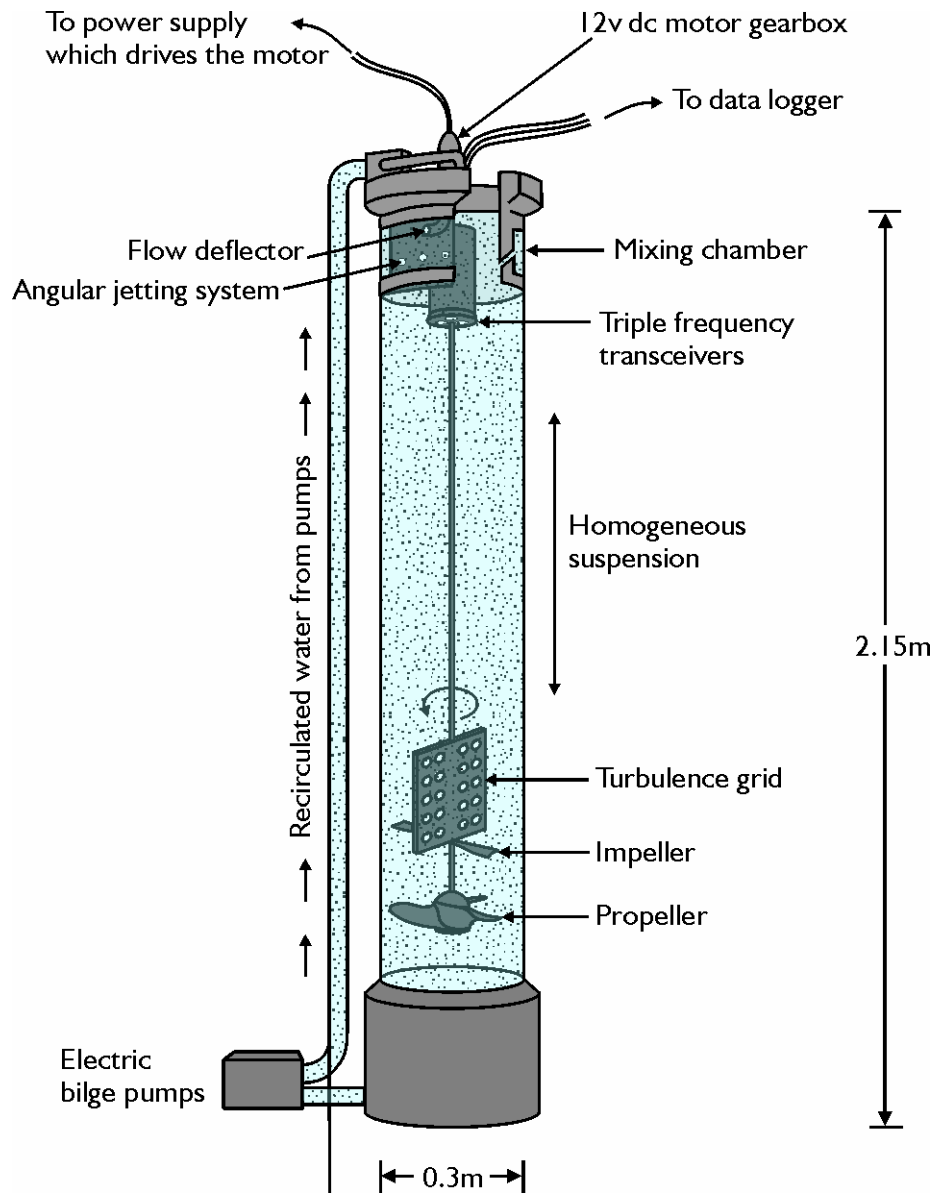
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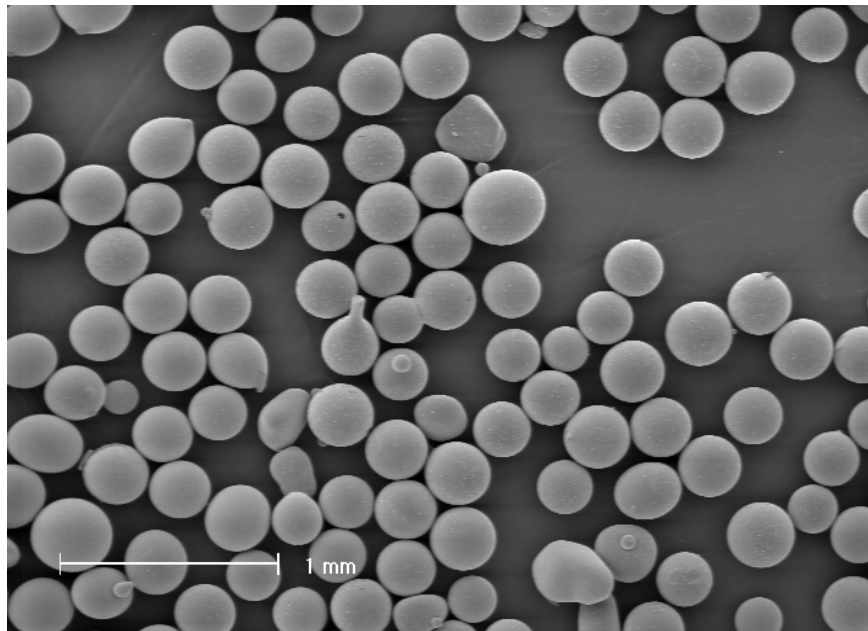


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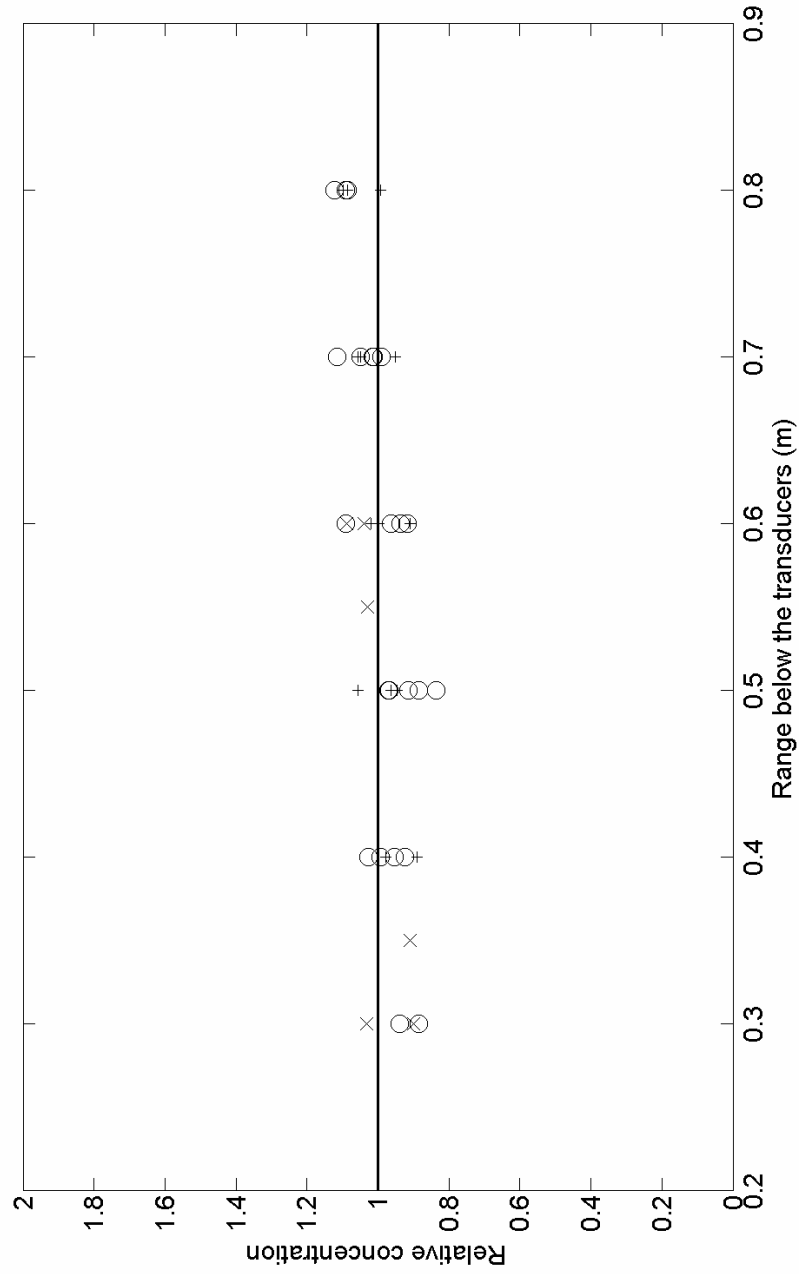
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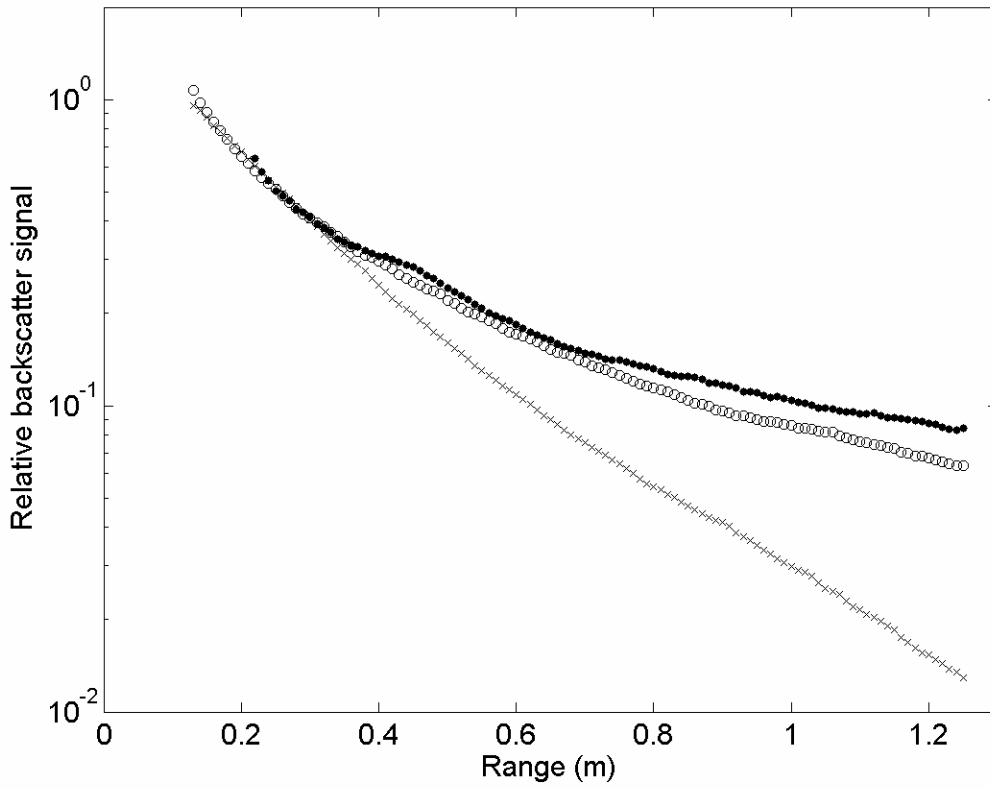


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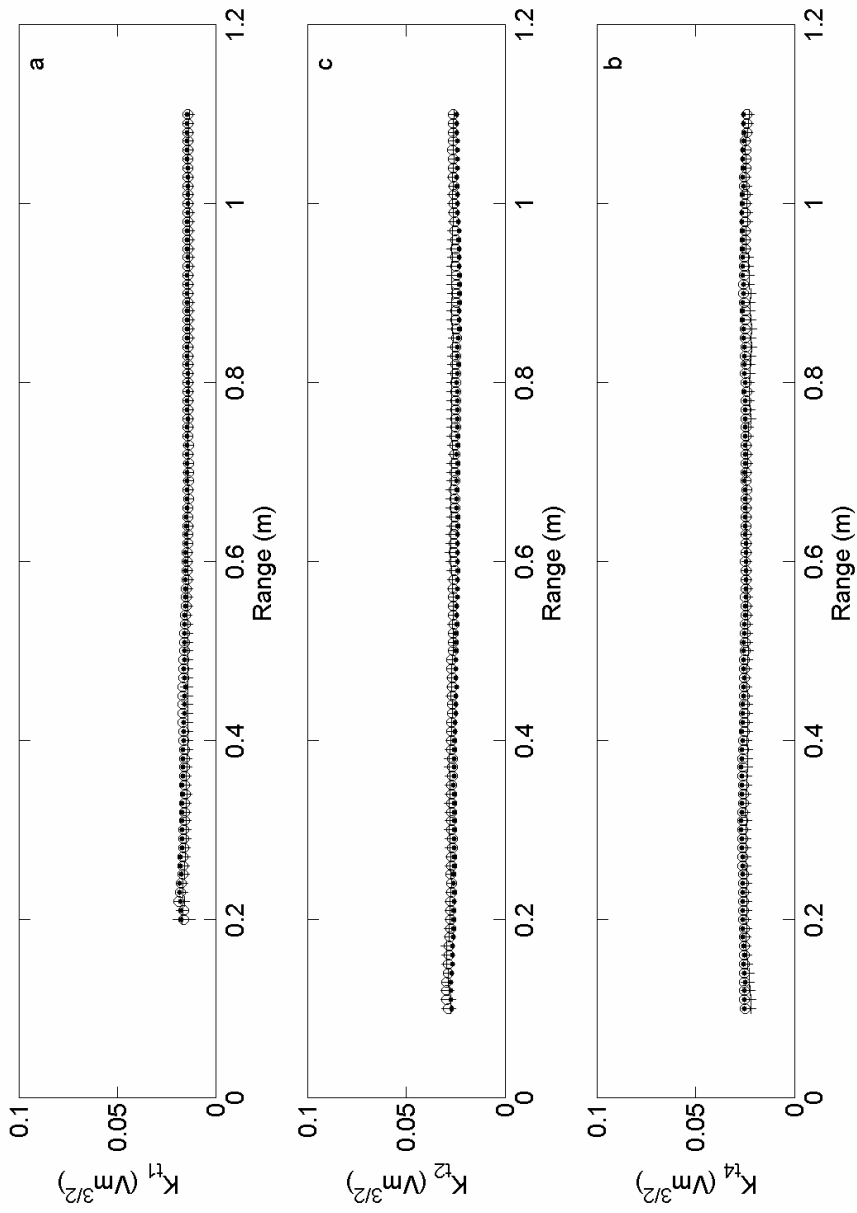


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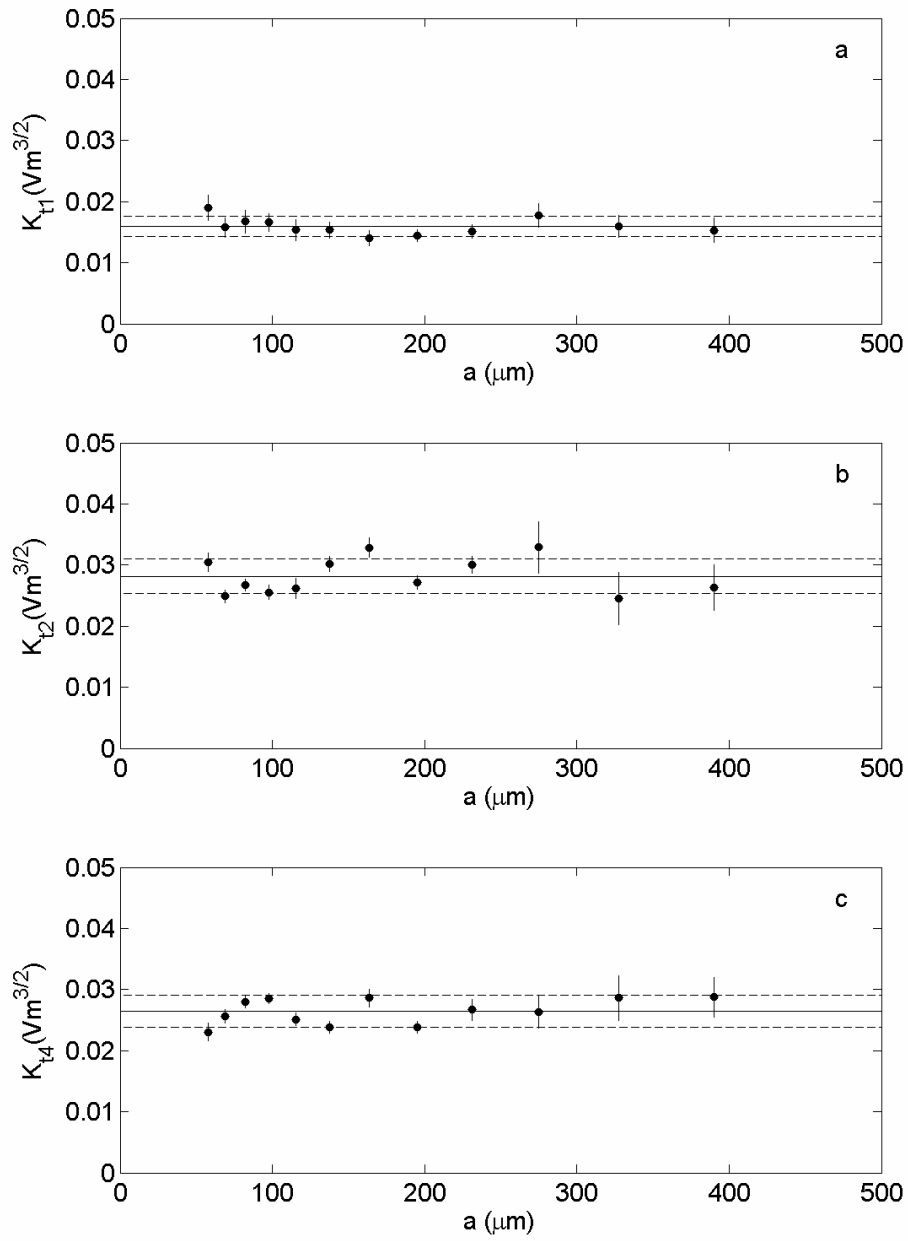
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